

UNIVERSITY OF AMSTERDAM Informatics Institute



# Machine Learning 1

Lecture 5.4 - Supervised Learning Classification - Decision Regions

Erik Bekkers

(Bishop 1.5, 4.1)

Slide credits: Patrick Forré and Rianne van den Berg

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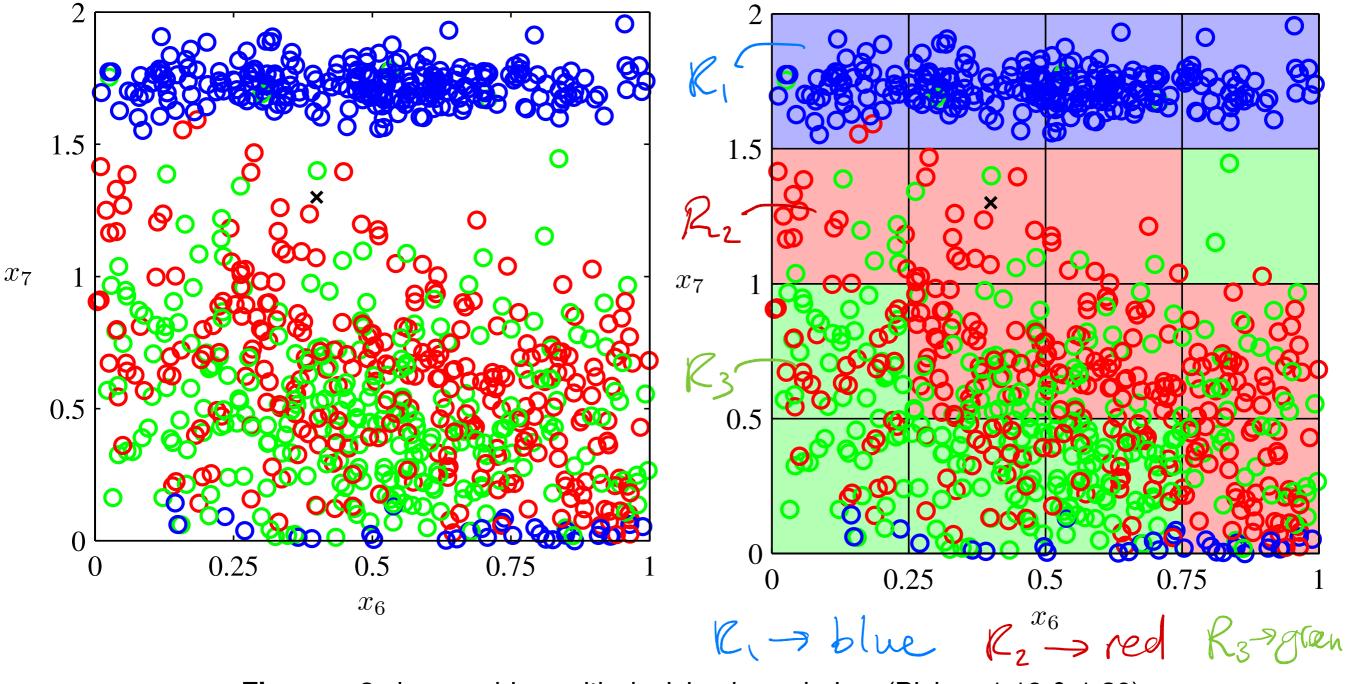
### Classification through decision regions

- Input:  $\mathbf{x} = (x_1, ..., x_D)^T$
- Target:  $E \in \{C_1, C_2, \ldots, C_k\}$ 
  - 2-class targets:  $t = C_1$ ,  $t = C_2$   $\leftarrow > t = 0$ , t = 1

#### **Strategy:**

- Divide input space  $\mathbb{R}^{D}$  into K decision regions.  $\mathcal{R}_{k}$
- Assign each decision region to a class
- Boundaries of decision regions are called decision boundaries/surfaces.

### **Classification through Decision Regions**

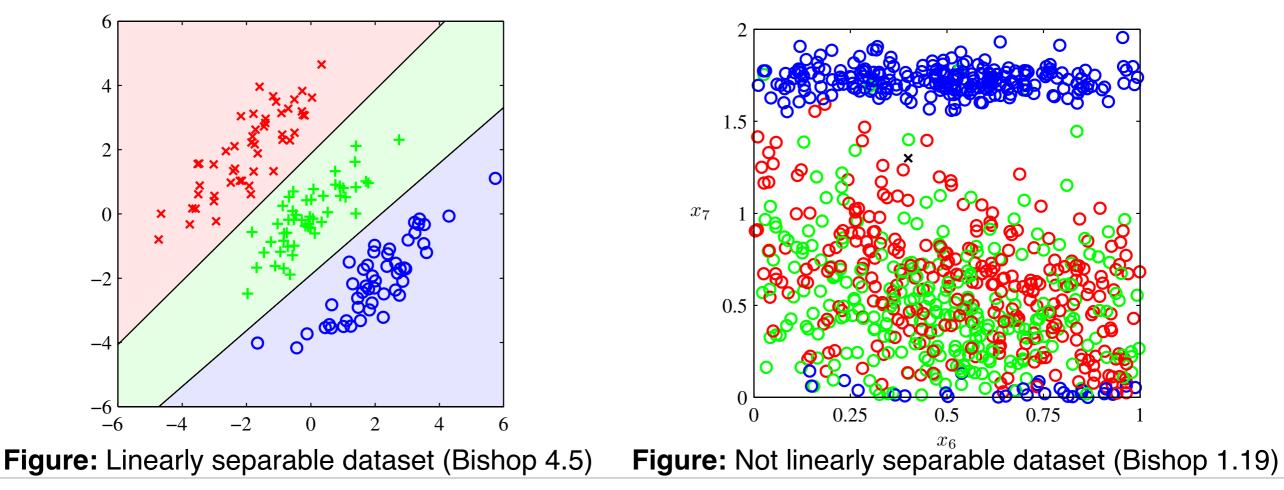


Figures: 3 class problem with decision boundaries. (Bishop 1.19 & 1.20)

K = 2

## Linear Classification

- Linear Classification: consider only *linear* decision boundaries
- For *D* dimensional input space:  $\simeq \in \mathbb{R}^p$ decision surface is a  $\mathbb{P}_{-1}$  dimensional hyperplane
- Datasets whose classes can be separated exactly by linear decision surfaces are called *Linearly Separated*



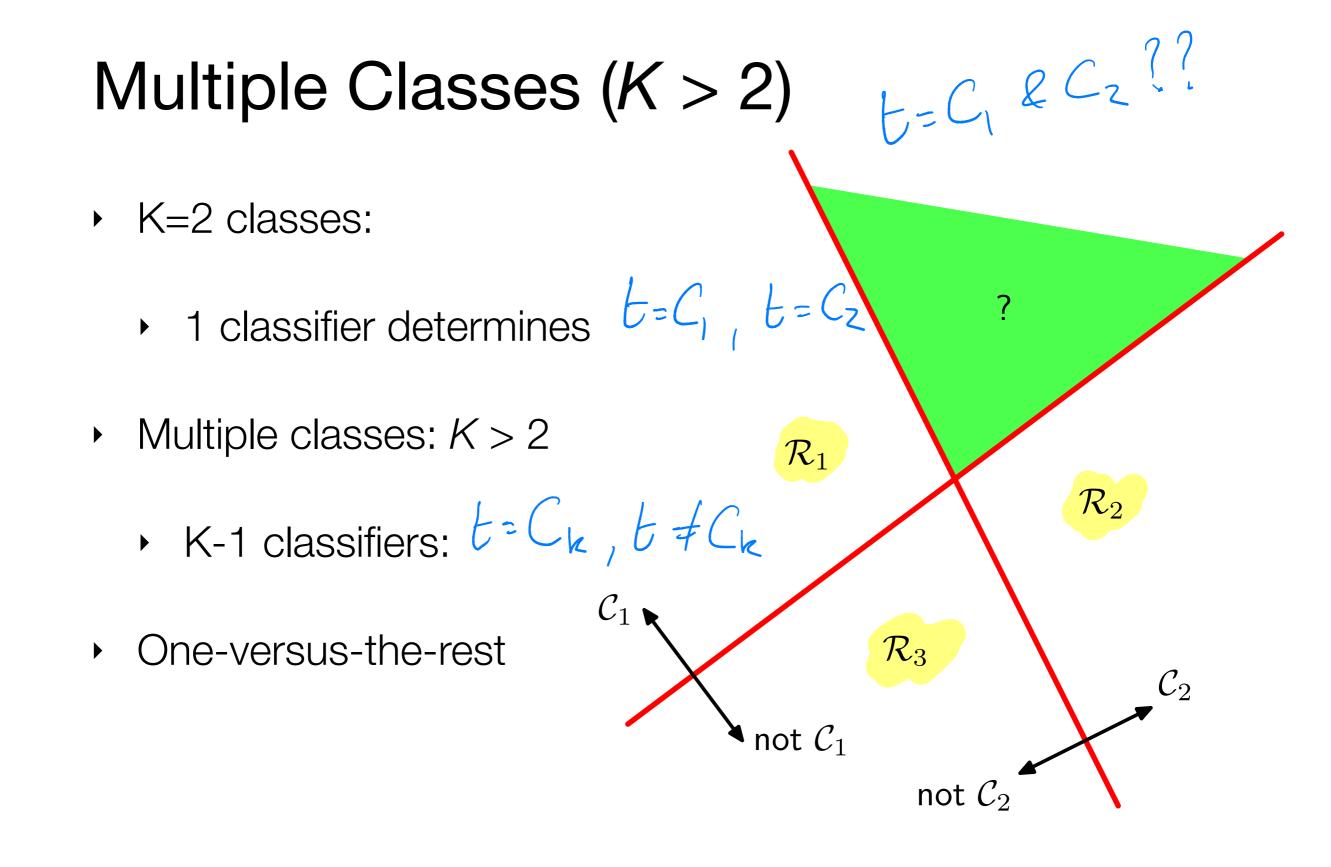
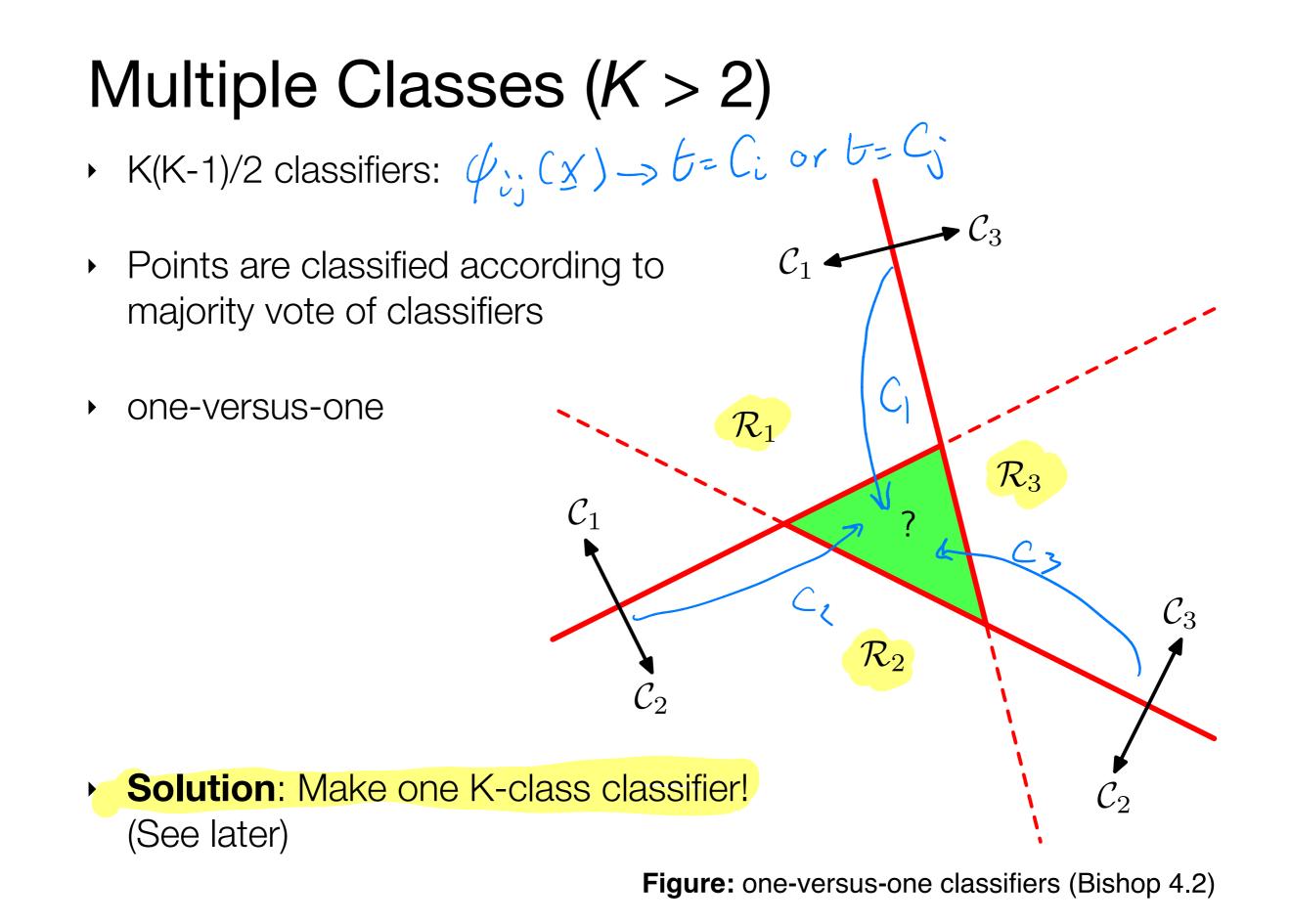


Figure: one-versus-the-rest classifiers (Bishop 4.2)



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